## A Spatial Discrete Choice Model of Crime

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## What we do...

- The causal relationship between proactive policing (in the sense of more time of police presence) and the incidence of crime is not yet well established.
- We use a unique experimental data set to identify the causal impact of police patrolling on crime. We exploit an identification strategy based on a random utility model of crime location choice.
- We estimate own-and cross-elasticities of crime to patrolling time and we were able to evaluate alternative patrolling strategies.


## Results

- Our estimates show that $1 \%$ more time patrolling reduces crime an average of $0.19 \%$. Cross-price elasticities show little support to negative spillover effects of police patrolling.
- Allocating police time according to crime incidence and the elasticities of each quadrant, could potentially reduce violent crime by $4.13 \%$ and property crime by $6 \%$.


## Motivation

- Crime prediction is now ubiquitous in crime prevention and police resource planning.
- There is already a vast literature.
- Equilibrium interaction (endogeneity): The optimal allocation of police resources is guided by police deployment strategies (e.g., prediction models), which at the same time determine what crime incidents are reported or how crime is displaced from one sector to another.


## Literature

- The evidence on the effects of proactive policing is mixed (see National Academies of Sciences y Medicine (2018) for a comprehensive study for the US).
- Braga y col. (2015) Identified 30 randomized experimental suggesting that policing disorder strategies are associated with an overall statistically significant modest crime reduction.
- Telep y col. (2014) Reviewed 19 publications covering 20 quasi-experimental studies. They found no significant overall evidence of displacement or a diffusion of benefits.
- Ratcliffe y col. (2011) reported the results of a randomized controlled trial of police effectiveness across 60 violent crime hot spots in Philadelphia. Their results suggested a significant reduction in the level of violent crime for the treated area after 12 weeks. Targeted areas outperformed the control sites by $23 \%$.


## Literature

- Novak y col. (2016) examined the effectiveness of foot patrol in violent micro-places in Kansas City. Their results reveal statistically significant short-run reductions in violent crime in the micro-places receiving foot patrol treatment. They found no evidence of crime displacement to spatially contiguous areas.
- Fitzpatricka y col. (2020) conducted a controlled field experiment of police placed-based interventions on violent crime. They found statistically significant reductions in serious violent crime counts within treatment hot spots as compared to control hot spots, with an overall reduction of $25.3 \%$ in violent crimes such as homicides, rape, robbery, and aggravated assault.


## Literature

- Blattman y col. (2021), a placed-based police and city services intervention at scale for Bogotá D.C., Colombia. The authors randomly assigned 1,919 streets to an 8-month treatment of doubled police patrols, greater municipal services, both, or neither. They found that increasing state presence has modest direct impacts. Confidence intervals suggest they can rule out total reductions in crime of more than $2 \%$.


## Literature

- In Bernasco y Nieubeerta (2005), the authors studied the selection of crime (burglary) locations in the city of The Hague, Netherlands. They used sociodemographic data of 290 burglars who committed 548 burglaries in the city during the period 1996-2001. They estimated a random utility model with burglars' and burglaries' characteristics by means of a conditional logit model. There is no causal identification of the effect of police patrolling on crime.


## Contribution

(1) We use a unique large data set of experimental data that allows for the identification of the causal effect of police patrolling on crime.
(2) Our identification strategy is based on random utility selection of spatial locations for crime.
(3) We used double selection techniques for a more agnostic data-driven model specification and robustness check of our results.
(9) We computed the police own- and cross-elasticity of crime for each of the quadrants
(6) Counterfactual strategies without increasing the total police time available: (a) uniformly across quadrants, (b) proportional to the incidence of crimes, (c) such that the more insecure and elastic quadrants receive either a 10 $100 \%$ increase, and (d) recursively increasing $1 \%$ of patrol time for the most insecure and elastic quadrant.

## Spatial Discrete Choice Model

- Consider $N$ potential criminal offenders with symmetric preferences, each of them deciding between $J+1$ locations in the city to commit a crime.
- Each potential offender bases her location choice on her perceived utility of committing a crime in each of the $J+1$ locations.
- The associated utility $u_{i j}$, of agent $i$, of selecting location $j$, is given by

$$
\begin{equation*}
u_{i j}=\alpha P_{j}+X_{j} \beta+\xi_{j}+\varepsilon_{i j} \tag{1}
\end{equation*}
$$

where $P_{j}$ is a measure of the police presence in location $j, X_{j}$ is a vector of $K$ observed characteristics of the location, $\xi_{j}$ is the unobserved characteristics of location $j, \varepsilon_{i j}$ is the idiosyncratic error term.

## Spatial Discrete Choice Model

- Assuming $\varepsilon_{i j}, \varepsilon_{i j^{\prime}}$ are i.i.d. extreme value type I distributed, location choice probabilities have a closed-form expression given by

$$
\begin{equation*}
s_{i j}\left(P_{j}, X_{j}, \xi_{j} ; \alpha, \beta\right)=\frac{\exp \left(\delta_{j}\right)}{1+\sum_{k=1}^{J} \exp \left(\delta_{k}\right)} \tag{2}
\end{equation*}
$$

where option $j=0$ is assumed to be the outside option and $\delta_{j}=\alpha P_{j}+X_{j} \beta+\xi_{j}$.

- Due to the assumed symmetry of preferences it follows that the share of committed crimes at location $j$ :

$$
S_{j}\left(P_{j}, X_{j}, \xi_{j} ; \alpha, \beta\right)=s_{i j}\left(P_{j}, X_{j}, \xi_{j} ; \alpha, \beta\right)
$$

## Spatial Discrete Choice Model

- Own- and cross-elasticities of crime with respect to police presence $P_{j}$ (or any observed characteristic $x_{r j} \in X_{j}$ ) are given by

$$
\frac{\partial S_{j}}{\partial P_{\ell}}= \begin{cases}\alpha S_{j}\left(1-S_{j}\right) & \text { if } j=\ell  \tag{3}\\ -\alpha S_{j} S_{\ell} & \text { if } j \neq \ell\end{cases}
$$

and thus, the police own- and cross-elasticities of crime are

$$
E_{S_{j}, P_{\ell}} \equiv \frac{\partial S_{j}}{\partial P_{\ell}} \frac{P_{\ell}}{S_{j}}= \begin{cases}\alpha\left(1-S_{j}\right) P_{j} & \text { if } j=\ell  \tag{4}\\ -\alpha S_{\ell} P_{\ell} & \text { if } j \neq \ell\end{cases}
$$

## Estimation

- To estimate the structural parameters $\theta=(\alpha, \beta)$ from equation (1) we note that:

$$
\begin{equation*}
\delta_{j}=\log \left(S_{j}\right)-\log \left(S_{0}\right)=\alpha P_{j}+X_{j} \beta+\xi_{j} \tag{5}
\end{equation*}
$$

## Estimation: Endogeneity

Violent crimes


Total crimes


## Property crimes



## Estimation: TSLS

- Starting in January 2016 and during 8 months, 756 out of 1,919 street segments labeled as crime hot spots - out of the 136,984 street segments of the city - received a doubled patrolling time (92-167 minutes of police patrol per day) Blattman y col. (2021).
- In March 2016, 201 of the 1,919 hot spots received more intensive street light repair and cleaning Blattman y col. (2021).
- We used the first type of treatment to instrument the police presence $P_{j}$ and identify the structural parameters of interest. That is, we estimate equation (5) by TSLS.


## Estimation: TSLS

- The necessary assumptions for the treatment assignment, $Z$, to be a valid instrument are:
(1) Independence.
(2) Exclusion restriction: $Z$ only affects $\delta_{j}$ through $P_{j}$.
(3) Rank condition (relevance): "police complied with their new orders for the full 8 months.".
(1) Monotonicity (no defiers): police officers were monitored via GPS every 30 seconds and police officers plausibly double their efforts in a task only when they are ordered.


## Estimation: Double Selection

- To select the variables that should be included in $X_{j}$ we implemented the double selection methodology of Belloni y col. (2014).
- We first (separately) ran a regularized lasso over the following two equations:

$$
\begin{align*}
\delta_{j} & =\tilde{X}_{j} \gamma+\mu_{j},  \tag{6}\\
P_{j} & =\tilde{X}_{j} \vartheta+\lambda_{j}, \tag{7}
\end{align*}
$$

where $\tilde{X}_{j}$ is a vector of variables that includes all the available and exogenous location features and all their second degree interaction terms, while $\mu_{j}$ and $\lambda_{j}$ are the error terms.

## Results: Estimation

## Table 4: TSLS $\beta$ estimates for double-selection selected covariates that predict $\delta_{j}$

|  | Violent Crimes <br> $(1)$ | Property Crimes <br> $(2)$ | Total Crimes <br> $(3)$ |
| :--- | :---: | :---: | :---: |
| Avg. dist. to nearest shopping center | - | -0.001 | - |
|  | - | $(0.001)$ | - |
| Avg. dist. to nearest shopping center $\times$ | - | -0.0001 | - |
| Prop. of paved segments | - | $(0.001)$ | - |
|  |  |  |  |
| $N$ | 1,018 | 1,018 | 1,018 |
| Adj. $R^{2}$ | 0.307 | 0.396 | 0.216 |

Notes: ${ }^{*} \mathrm{p}<0.1 ;{ }^{* *} \mathrm{p}<0.05 ;{ }^{* * *} \mathrm{p}<0.01$. Heteroskedasticity robust standard errors in parentheses (HC1). Double-selection selected variables that explain $P_{j}$ excluded since there were 89 selected variables and their interpretation would be cumbersome. Avg.: Average. Prop.: Proportion. Dist.: distance

Table 5：Double－selection selected covariates that predict $P_{j}$
 form．Panel B presents check marks $(\checkmark)$ for the quadratic double－selection selected variables．In this case，a check mark in row $\ell$ and column $m$ indicates that the interaction between variables $\ell$ and $m$ was selected．No coefficients are displayed to avoid cumbersome interpretations．Panel B is a symmetric matrix of check marks．

## Results: Estimation

Table 2: $\alpha$ estimates from different econometric methodologies

|  | Violent Crimes <br> $(1)$ | Property Crimes <br> $(2)$ | Total Crimes <br> $(3)$ |
| :--- | :---: | :---: | :---: |
| A. OLS | -0.001 | $-0.003^{* * *}$ | $-0.002^{* * *}$ |
| $\alpha$ estimate | $(0.001)$ | $(0.001)$ | $(0.001)$ |
|  |  |  |  |
| N | 1,026 | 1,040 | 1,047 |
| Adj. R | 0.282 | 0.348 | 0.194 |
| B. Double Selection | -0.001 | $-0.002^{* * *}$ | $-0.002^{* * *}$ |
| $\alpha$ estimate | $(0.001)$ | $(0.001)$ | $(0.001)$ |
|  |  |  |  |
| N | 1,018 | 1,018 | 1,018 |
| Adj. R |  | 0.316 | 0.404 |
| C. TSLS |  |  | 0.225 |
| $\alpha$ estimate | -0.002 | $-0.005^{* * *}$ | $-0.003^{* *}$ |
|  | $(0.001)$ | $(0.002)$ | $(0.001)$ |
| N |  |  |  |
| Adj. R ${ }^{2}$ | 1,026 | 1,040 | 1,047 |
| D. TSLS + Double Selection | 0.277 | 0.338 | 0.189 |
| $\alpha$ estimate | -0.003 | $-0.004^{* * *}$ | $-0.004^{* *}$ |
|  | $(0.002)$ | $(0.002)$ | $(0.001)$ |
| N |  |  |  |
| Adj. R ${ }^{2}$ | 1,018 | 1,018 | 1,018 |

## Results:Estimation


(a) Police elasticity of crime

## Results：Estimation


（b）Cross police elasticity of crime

## Results

## Table 6: Counterfactual analysis of different types of police patrol assignments

|  | Violent Crimes |  |  | Property Crimes |  |  | Total Crimes |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Bene N | $\begin{gathered} \text { ited Q. } \\ \% \end{gathered}$ | Predicted \# Mean (SD) |  | $\text { ited } Q \text {. }$ <br> \% | Predicted \# Mean (SD) | Bene N | $\begin{gathered} \text { ted Q. } \\ \% \end{gathered}$ | Predicted \# Mean (SD) |
| A. Base scenario |  |  |  |  |  |  |  |  |  |
| Observed | - | - | 12.31 | - | - | 24.61 | - | - | 36.92 |
|  | - | - | (8.51) | - | - | (17.89) | - | - | (21.18) |
| Predicted | - | - | 10.39 | - | - | 21.33 | - | - | 32.90 |
|  | - | - | (4.12) | - | - | (9.90) | - | - | (9.44) |
| B. Counterfactual scenarios |  |  |  |  |  |  |  |  |  |
| Uniform | 544 | 53.43 | 10.68 | 544 | 53.43 | 22.64 | 544 | 53.43 | 34.37 |
|  |  |  | (4.12) |  |  | (11.12) |  |  | (10.22) |
| Proportional time | 514 | 50.49 | 10.40 | 511 | 50.19 | 21.73 | 516 | 50.68 | 33.39 |
|  |  |  | (4.15) |  |  | (11.03) |  |  | (11.03) |
| Reassignment 3 |  |  |  |  |  |  |  |  |  |
| $0 \%$ increase (Base case) | 0 | 0.00 | 10.39 | 0 | 0.00 | 21.33 | 0 | 0.00 | 32.90 |
|  |  |  | (4.12) |  |  | (9.90) |  |  | (9.44) |
| 10\% increase | 809 | 79.47 | 10.36 | 776 | 76.23 | 21.23 | 742 | 72.89 | 32.89 |
|  |  |  | (4.06) |  |  | (9.70) |  |  | (9.37) |
| $20 \%$ increase | 664 | 65.23 | 10.36 | 621 | 61.00 | 21.20 | 585 | 57.47 | 32.93 |
|  |  |  | (4.06) |  |  | (9.63) |  |  | (9.47) |
| $30 \%$ increase | 565 | 55.50 | 10.36 | 514 | 50.49 | 21.20 | 475 | 46.66 | 33.01 |
|  |  |  | (4.05) |  |  | (9.64) |  |  | (9.64) |
| $40 \%$ increase | 475 | 46.66 | 10.38 | 427 | 41.94 | 21.25 | 400 | 39.29 | 33.08 |
|  |  |  | (4.09) |  |  | (9.71) |  |  | (9.81) |
| 50\% increase | 421 | 41.36 | $10.38$ | 359 | 35.27 | $21.29$ | 339 | 33.30 | $33.15$ |
|  |  |  | $(4.09)$ |  |  | $(9.75)$ |  |  | (9.99) |
| $60 \%$ increase | 371 | 36.44 | $10.39$ | 313 | 30.75 | $21.35$ | 293 | 28.78 | $33.22$ |
|  |  |  | $(4.12)$ |  |  | $(9.85)$ |  |  | $(10.12)$ |
| 70\% increase | 329 | 32.32 | 10.41 | 277 | 27.21 | 21.40 | 259 | 25.44 | 33.29 |
|  |  |  | (4.16) |  |  | (9.94) |  |  | (10.20) |
| $80 \%$ increase | 294 | 28.88 | 10.44 | 252 | 24.75 | 21.44 | 232 | 22.79 | 33.41 |
|  |  |  | (4.21) |  |  | (10.01) |  |  | (10.51) |
| $90 \%$ increase | 272 | 26.72 | 10.44 | 221 | 21.71 | 21.53 | 214 | 21.02 | 33.46 |
|  |  |  | (4.23) |  |  | (10.13) |  |  | (10.64) |
| 100\% increase | 245 | 24.07 | 10.45 | 200 | 19.65 | 21.60 | 192 | 18.86 | 33.56 |
|  |  |  | (4.26) |  |  | (10.24) |  |  | (10.83) |
| Reassignment 4 | 513 | 50.39 | 9.96 | 538 | 52.84 | 20.04 | 636 | 62.47 | 32.00 |
|  |  |  | (2.80) |  |  | (5.97) |  |  | (5.43) |

## Results

## Violent crimes



Total crimes


Property crimes


## Conclusions

- Our estimates show that $1 \%$ more time patrolling reduces crime an average of $0.19 \%$.
- Cross-price elasticities show little support to negative spillover effects of police patrolling.
- Allocating police time according to crime incidence and the elasticities of each quadrant, could potentially reduce violent crime by $4.13 \%$ and property crime by $6 \%$.

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